

Long-lived neutral-kaon flux measurement for the KOTO experiment

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 The KOTO (K^0 at Tokai) experiment aims to observe the CP-violating rare decay $K_L \rightarrow \pi^0 \nu \bar{\nu}$ by using a long-lived neutral-kaon beam produced by the 30 GeV proton beam at the Japan Proton Accelerator Research Complex. The K_L flux is an essential parameter for the measurement of the branching fraction. Three K_L neutral decay modes, $K_L \rightarrow 3\pi^0$, $K_L \rightarrow 2\pi^0$, and $K_L \rightarrow 2\gamma$ were used to measure the K_L flux in the beam line in the 2013 KOTO engineering run. A Monte Carlo simulation was used to estimate the detector acceptance for these decays. Agreement was found between the simulation model and the experimental data, and the remaining systematic uncertainty was estimated at the 1.4% level. The K_L flux was measured as $(4.183 \pm 0.017_{\text{stat.}} \pm 0.059_{\text{sys.}}) \times 10^7$ K_L per 2×10^{14} protons on a 66-mm-long Au target.

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1. Introduction

The KOTO (K^0 at Tokai) experiment is aimed at the first observation of the rare CP-violating decay of the long-lived neutral-kaon $K_L \rightarrow \pi^0 \nu \bar{\nu}$. An important characteristic of this decay is its theoretical cleanness. The branching fraction (BF) is predicted to be 2.4×10^{-11} with a theoretical uncertainty of only 2.5% [1], in contrast to that of most other meson decays, especially in the B system, where the uncertainty can be as high as 10%. The study of $K_L \rightarrow \pi^0 \nu \bar{\nu}$ can also shed light on the origin of CP violation as it provides a direct precise measurement of the parameter η [2], the height of the unitarity triangle, in the standard model (SM) of particle physics. In addition, $K_L \rightarrow \pi^0 \nu \bar{\nu}$ involves an $s \rightarrow d$ transition that is highly suppressed in the SM and thus is very effective in searching for new physics that modifies the SM flavor structure. The current experimental upper limit on the BF is 2.6×10^{-8} at the 90% confidence level, obtained by the KEK-E391a experiment [3] at the KEK 12 GeV proton synchrotron (KEK-PS).

The KOTO experiment [4] uses the experimental technique established by E391a. In order to improve the sensitivity by three orders of magnitude, a new dedicated beam line was constructed at the Japan Proton Accelerator Research Complex (J-PARC) [5]. The design value of the proton intensity delivered by the Main Ring (MR) at J-PARC is 100 times higher than that of the KEK-PS. To improve the background suppression, the main electromagnetic calorimeter and other detectors surrounding the decay volume were upgraded.

The K_L flux generated by the proton beam is an essential parameter for the measurement of the BF of $K_L \rightarrow \pi^0 \nu \bar{\nu}$. The KOTO Collaboration measured the K_L flux and the momentum spectrum by reconstructing the charged decay modes $K_L \rightarrow \pi^+ \pi^- \pi^0$ and $K_L \rightarrow \pi^+ \pi^-$ in beam surveys with dedicated tracking detectors and calorimeters [6, 7]. During data acquisition, the K_L flux is measured using the neutral decay modes $K_L \rightarrow 3\pi^0$, $K_L \rightarrow 2\pi^0$, and $K_L \rightarrow 2\gamma$, since the KOTO detector cannot measure the momentum of charged pions. In this paper, we report on KOTO's first measurement of the K_L flux by using the three neutral decay modes with the main calorimeter, which was performed during an engineering run in January 2013.

The paper is organized as follows. Section 2 describes the experimental setup relevant to the measurement. Section 3 illustrates the principle and the technique used in the measurement. Section 4 reports on the Monte Carlo (MC) simulation used to measure the acceptance of each of the three modes. Section 5 describes the analysis of the experimental data for each of the three modes. Section 6 reports the results and their uncertainty estimations. Section 7 compares this to previous results. Section 8 describes the conclusions.

2. Experimental setup

This section focuses on the experimental setup used for the measurement, including descriptions of the beam line and of the subsystems in the KOTO detector relevant for this analysis.

2.1. Beam Line

The KOTO detector is located at the Hadron Experimental Facility of J-PARC, at the end of a new 21-m-long neutral-kaon beam line (KL). A schematic top view of the KL beam line and the KOTO detector is shown in Fig. 1. The protons are accelerated to 30 GeV by

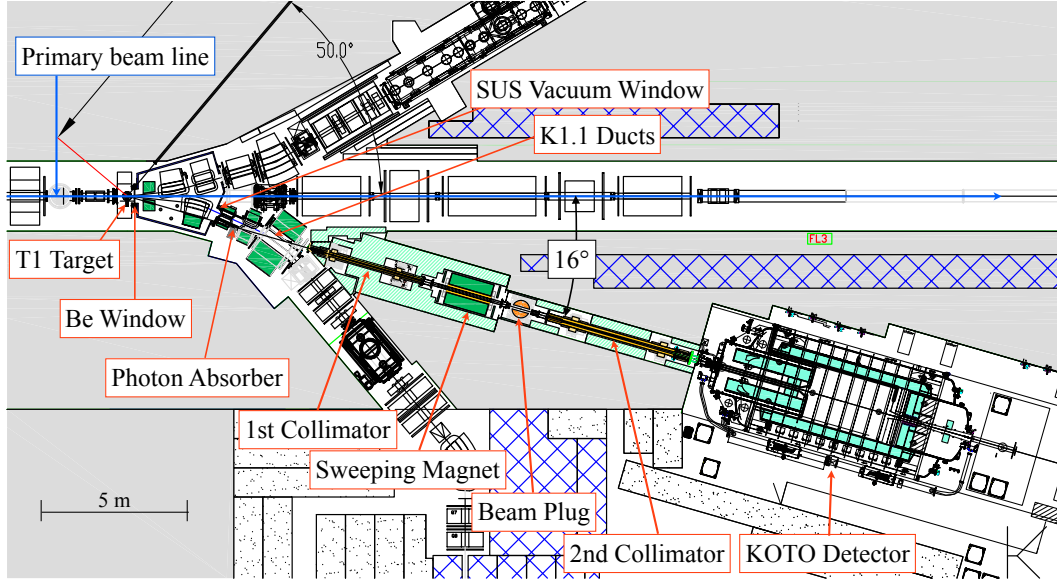


Fig. 1: Schematic top view of the KL beam line used by the KOTO experiment. The primary proton beam comes in from the left. The KL beam line starts at the T1 target and the beam axis goes off at an angle of 16° with respect to the primary beam line. The front of the KOTO detector is located at the end of the beam line, about 21 m from the T1 target.

the MR, extracted by using a slow extraction technique [8], and transported through the primary beam line to the facility [9]. The proton beam intensity is monitored by a secondary emission chamber (SEC), located after the extraction point. The primary proton beam, with a cross section of approximately 1 mm in radius, is injected into the production target (T1). The target consists of a 66-mm-long gold target of $6 \times 6 \text{ mm}^2$ cross section. It is equally divided into six parts along its length with five 0.2-mm-thick slits.

The KL beam line is off-axis by an angle of 16° with respect to the primary proton beam line. The full kinematic reconstruction of the neutral pion in the $K_L \rightarrow \pi^0 \nu \bar{\nu}$ decay requires a small diameter for the K_L beam and was achieved with the collimation scheme shown in Fig. 2. The secondary particles produced at the target pass through the pair of collimators shown in Fig. 2 to shape the beam. At the exit of the second collimator, the neutral beam has a square cross-section of $8.5 \times 8.5 \text{ cm}^2$ corresponding to a solid angle of $7.8 \text{ } \mu\text{sr}$. Before entering the collimation region, the beam passes through a 7-cm-thick ($12.5 X_0$) lead absorber which removes most of the photons. A 2-T dipole magnet, located between the two collimators sweeps out charged particles. Short-lived particles decay in the long collimator region leaving only K_L mesons, neutrons, and photons at the entry of the detector region. Table 1 lists the composition and location of all the components along the KL beam line. The materials in the beam decrease the K_L flux by 60%, as estimated using a Geant4 [10, 11] based MC simulation. The collimation scheme of the KL beam line is described in Ref. [12].

2.2. KOTO detector

Figure 3 shows a cross-sectional side view and the coordinate system of the KOTO detector. The signature of a $K_L \rightarrow \pi^0 \nu \bar{\nu}$ decay is a pair of photons coming from the π^0 decay, without

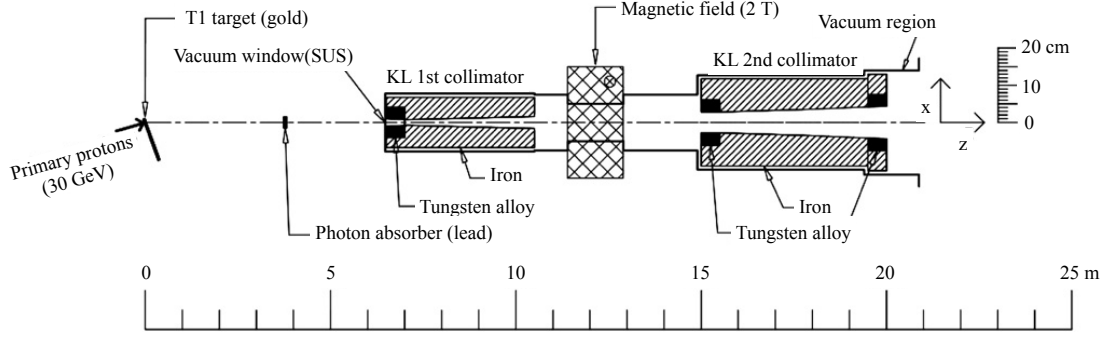


Fig. 2: KOTO collimation scheme in the beam line coordinates [12].

Table 1: Composition and position of materials along the axis of the KL beam line: some components are part of the K1.1 charged-kaon beam line, which uses the same T1 target and is at an angle of 7° with respect to the KL beam line. The thickness is listed only for materials actually crossed by the beam. The regions between the Be vacuum window and the stainless steel vacuum window, and between the K1.1 front duct and the beam exit window are in a 2-Pa vacuum. The starting position is in beam line coordinates, whose origin is at the center of the T1 target. The KOTO detector starts at the front face of the Front Barrel; detector coordinates are measured with respect to this position.

Name	Material	Thickness [mm]	Starting position [mm]
T1 target	Au	66	-
Vacuum window	Be	8	247
Vacuum window	Stainless steel	0.2	3,097
Photon absorber	Pb	70	3,730
K1.1 front duct	Stainless steel	0.2	4,182
K1.1 tail duct	Stainless steel	0.2	5,510
Collimator vacuum window	Stainless steel	0.1	6,400
1 st collimator	Fe and W alloy	-	6,500
2 nd collimator	Fe and W alloy	-	15,000
Beam exit vacuum window	Polyimide	0.125	20,000
Front Barrel	-	-	21,507
CsI calorimeter	-	-	27,655

any other detectable particles. The energy and position of the two photons are measured with a cesium iodide electromagnetic calorimeter (CsI) [13]. Multiple charged-particle and photon detectors surround the decay volume to form a hermetic veto against any extra particles except neutrinos. The decay vertex of the K_L is reconstructed under the assumption that the two photons come from a π^0 on the beam axis and that the vertices of the K_L and π^0 coincide. Finally the π^0 is required to have a large transverse momentum to balance the momentum carried by the two neutrinos.

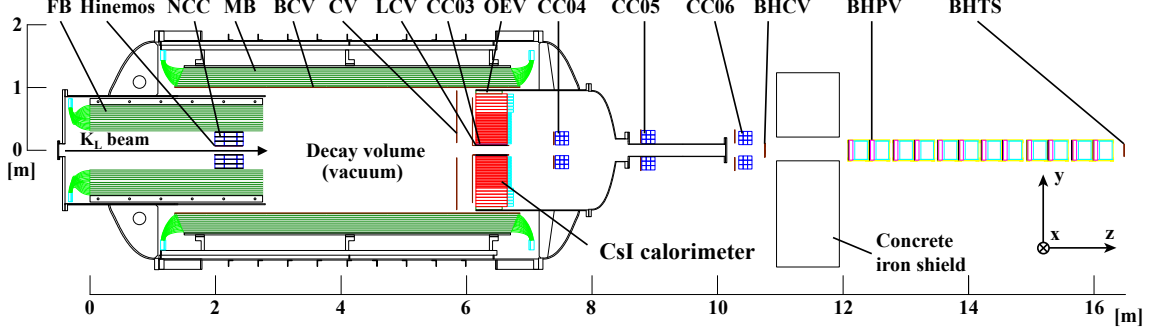


Fig. 3: Cross-sectional side view of KOTO in detector coordinates, defined with respect to the front face of the Front Barrel (FB) detector. K_L particles come in from the left. The z -axis is along the beam direction, the y -axis points upward, and the x -axis goes into the page. The CsI calorimeter, located downstream of the decay volume, is surrounded by two photon detectors (FB and MB), charged-particle veto detectors (CV, LCV, BCV, and Hinemos), photon veto collar counters made of CsI crystals (NCC, CC03, CC04, CC05, and CC06) and forward charged-particle and photon detectors (BHCV and BHPV). The gap between the MB and the CsI calorimeter is filled with a photon detector (OEV). BHTS is a trigger scintillator which is used for detector performance checks.

For this K_L flux measurement, in addition to the CsI calorimeter, the Main Barrel (MB) [14] and the Charged Veto (CV) [15], which are described below, are used as veto detectors.

The CsI calorimeter consists of 2716 undoped CsI crystals stacked in a cylindrical shape of 2-m diameter and 500-mm depth ($27 X_0$) along the beam direction. We use crystals of two sizes: 2240 small crystals of $25 \times 25 \text{ mm}^2$ cross section for the inner region and 476 large crystals of $50 \times 50 \text{ mm}^2$ for the outer region. The calorimeter has a $148 \times 148 \text{ mm}^2$ square beam hole at its center. The CsI crystals have a typical light yield of 9 photoelectrons (p.e.)/MeV, and an energy resolution σ_E/E of $1.9\%/\sqrt{E [\text{GeV}]}$ with a constant term of 0.6%. They are read out by photomultiplier tubes (PMTs) [16].

The MB is a cylindrical photon veto detector 5.5 m long with 2-m inner diameter surrounding the decay volume. It consists of 32 modules, each made of 45 alternate layers of plastic scintillator and lead sheet. The inner 15 layers have 1-mm-thick lead sheets while the outer 30 layers have 2-mm-thick lead sheets. The thickness of the plastic scintillator is 5 mm for both the inner and outer layers. The total thickness of the modules is $13.5 X_0$. The scintillation light originating in the plastic scintillator is absorbed by wavelength-shifting fibers (WLSFs) and read out by PMTs that are connected at both ends of each inner and outer module. Figure 4 shows a cross-sectional end view of the CsI calorimeter and the MB photon veto detector.

The CV is the main charged-particle veto detector. It consists of two layers, placed 5 cm and 30 cm upstream of the calorimeter. Each layer is made of 3-mm-thick and 69-mm-wide plastic scintillator strips of lengths between 490 and 1002 mm, assembled as shown in Fig. 5. The scintillation light is picked up by WLSFs and read out by multi pixel photon counters

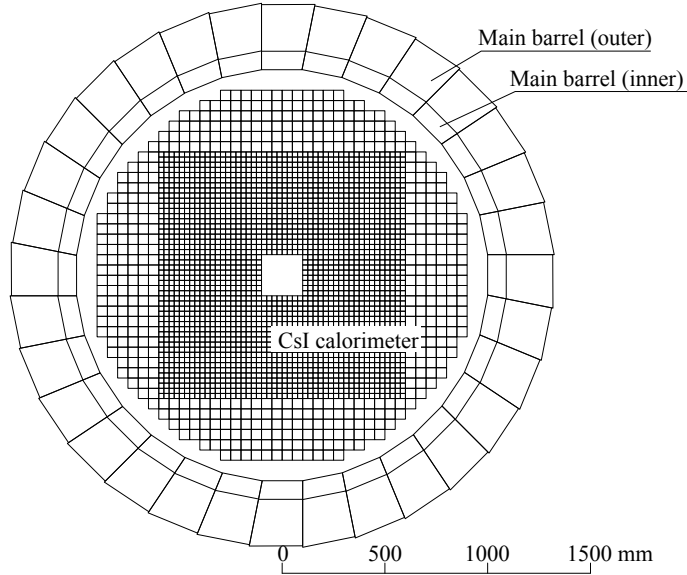


Fig. 4: Cross-sectional end view of the CsI calorimeter and the MB photon veto detector.

at both ends of each strip. The typical light yield of the strips is 186 p.e./MeV and the typical time resolution is 1.2 ns when averaging over the two ends [17].

These three detectors are all contained inside a pressure vessel defining the decay volume, which is evacuated to 10^{-3} Pa to suppress interactions of the beam particles with the residual gas. Due to a large amount of outgassing, the detectors inside the pressure vessel are separated from the high-vacuum region by a thin membrane and evacuated at a level of 1 Pa.

Analog signals from all detectors are digitized by ADC modules. A filter inside the ADC modules shapes the raw front-end signals into Gaussian pulses approximately 50 ns wide before digitizing them at a 125 MHz sampling rate and with 14 bit resolution [18]. The digitized waveforms are transmitted to the data acquisition (DAQ) system via optical links and processed by a three-tiered trigger system [19]. The waveform consists of 64 consecutive 8-ns samples around the signal region, corresponding to a 512-ns time window.

3. K_L flux measurement

We performed an engineering run in January 2013 to check the performance of the KOTO detector, including the data readout and peripheral slow control systems. In addition to the commissioning of the detector, the K_L beam flux with the detector in situ was measured. This section describes the principles of the K_L flux measurement, the run conditions under which the data were taken, and the triggers used during the run.

3.1. Measurement principle

We determined the K_L flux at the beam exit vacuum window (see Table. 1). The number of K_L s were counted by using the neutral decay modes, $K_L \rightarrow 3\pi^0$, $K_L \rightarrow 2\pi^0$, and $K_L \rightarrow 2\gamma$, which have large statistics. Their branching fractions are listed in Table 2. These decay modes have a common final-state configuration with all the decay products being photons.

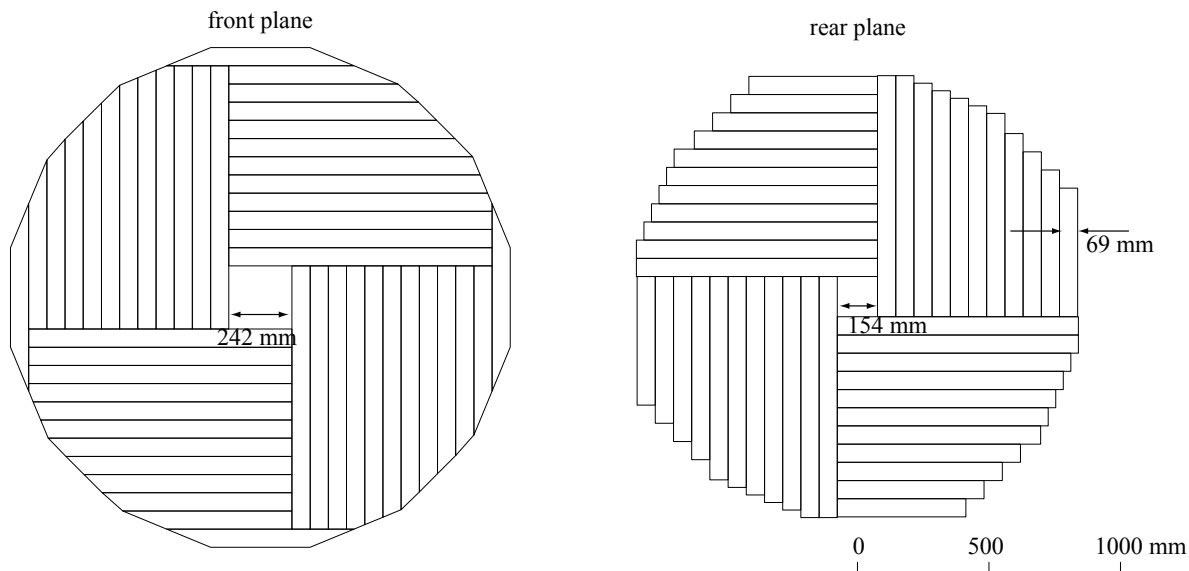


Fig. 5: End view of the CV detector showing the length and orientation of the 69 mm-wide plastic scintillator strips in each of the two CV layers.

Table 2: Branching fractions (BFs) of the three K_L neutral decay modes [20] used for the K_L flux measurement.

Mode	BF
$K_L \rightarrow 3\pi^0$	0.1952 ± 0.0012
$K_L \rightarrow 2\pi^0$	$(8.64 \pm 0.06) \times 10^{-4}$
$K_L \rightarrow 2\gamma$	$(5.47 \pm 0.04) \times 10^{-4}$

They provide three independent results that can be compared and cross-checked against each other.

The $K_L \rightarrow 2\gamma$ decays were reconstructed from events with only two photons assuming the nominal K_L mass. The $K_L \rightarrow 2\pi^0$ and $K_L \rightarrow 3\pi^0$ decays were reconstructed from two orthogonal sets of events with exactly four and six photons detected in the CsI calorimeter, respectively. To reconstruct the π^0 s, all possible combinations of two photon pairs were considered. The decay vertex position was calculated from the energy and position of the two photons in each pair, assuming the nominal π^0 mass. The photon pairing was determined by minimizing the variance of the common vertex position, as described in Sect. 5.3.1.

The MB inner layers were used as a photon veto to suppress the $K_L \rightarrow 3\pi^0$ background in the $K_L \rightarrow 2\pi^0$ and $K_L \rightarrow 2\gamma$ samples, when some of the photons fell outside the CsI fiducial area. The CV was used as a charged particle veto to remove backgrounds due to the $K_L \rightarrow \pi^\pm e^\mp \nu$ (K_{e3}) and $K_L \rightarrow \pi^+ \pi^- \pi^0$ decays by identifying charged-particles before they hit the CsI calorimeter.

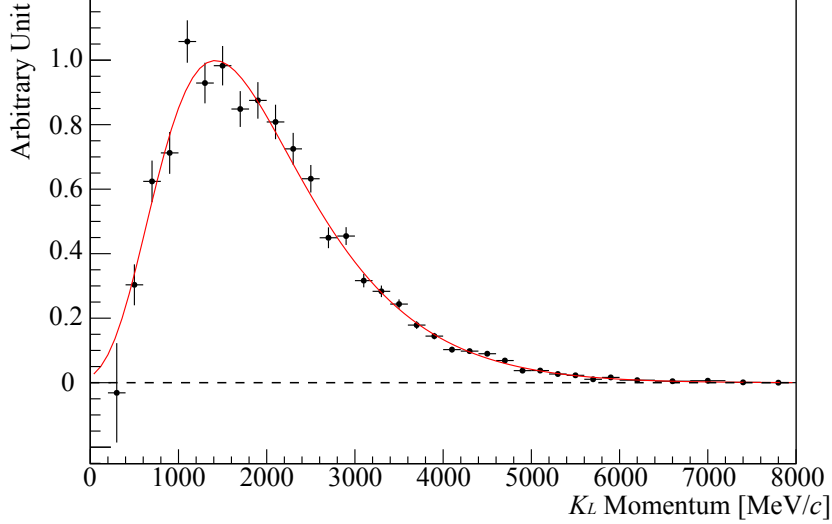


Fig. 6: K_L momentum distribution at the beam exit. Points with error bars are experimental data taken with a magnetic spectrometer [7]. The spectrum below 2000 MeV/ c was measured with $K_L \rightarrow \pi^+\pi^-$; that above 2000 MeV/ c was measured with $K_L \rightarrow \pi^+\pi^-$ and $K_L \rightarrow \pi^+\pi^-\pi^0$. The red curve is a Gaussian fit of the data with a momentum-dependent resolution and it is used to generate the K_L spectrum in the MC simulation. The fit returns a peak momentum of 1.42 GeV/ c .

3.2. Run condition

The data used for this analysis were accumulated during a 6-hour run taken on January 16, 2013. The nominal beam power was 15 kW, corresponding to an intensity of 1.8×10^{13} protons on target (POT) per spill. A spill had a duration of 2 s and a repetition rate of 6 s. The standard deviation of the beam intensity spill by spill was 0.7%. The total POT during the run, as measured by SEC, was $(3.355 \pm 0.013) \times 10^{16}$. The uncertainty was attributable mainly to the conversion factor from the SEC counts to POT.

3.3. Trigger

The K_L neutral decays used in the K_L flux measurement were triggered by requiring that the energy depositions in both the left and right halves of the CsI calorimeter be higher than a threshold. The common threshold for both halves of the calorimeter was 307.5 MeV, which resulted in a trigger rate of about 34 kHz. This trigger scheme is effective at selecting events with low missing energy.

4. Monte Carlo simulation

An MC simulation was used to estimate the acceptances of the detector for the $K_L \rightarrow 3\pi^0$, $K_L \rightarrow 2\pi^0$, and $K_L \rightarrow 2\gamma$ decays. It was also used to evaluate the contamination of background events from other K_L decays. The Geant4 MC package (Geant4.9.5.p02) was used to simulate the geometry of the KOTO detector and the interactions between particles and materials inside the detector. K_L particles were generated at the beam exit with the momentum spectrum shown in Fig. 6. The spectrum was measured independently in a special run with a magnetic spectrometer [7].

The detector response was corrected by using data taken in dedicated beam tests, bench tests with a ^{137}Cs radioactive source, and cosmic-ray runs with the detector in situ. For the CsI calorimeter, we added to the MC simulation the measured light yield of each crystal and its nonuniformity along the depth of the crystal, the accuracy of the energy calibration, the pedestal fluctuations, the light propagation velocity along the depth of the crystal, and the time smearing due to the timing resolution. For the MB photon veto, the length of the detector resulted in a substantial dependence of the light yield and timing delay on the position of the hit along the module. This effect was simulated by using a light propagation velocity and light attenuation measured in data (see Sect. 5.4.2). For the CV, the light yield and timing resolution measured for each strip were used in the simulation.

4.1. *Accidental overlay*

The overlap of accidental activity generated by simultaneous K_L decays or interactions of other beam particles was not simulated in the MC. Both of these accidental sources can result in additional energy deposition and possible distortion of the timing information recorded by the front-end electronics. To simulate such effects, we overlaid data collected with the accidental trigger described below to MC events passing the same selection criteria as the online trigger logic. The accidental data consisted of events triggered with the same trigger configuration described in Sect. 3.3, but recorded in a time window starting 512 ns or 768 ns before the actual trigger. The energy deposition measured in a randomly chosen accidental event was added to the energy deposition of a simulated event at the level of the ADC readout. If the energy of the overlapping event was larger than the energy of the simulated event, it determined the event timing at the detector.

5. Analysis

This section describes the calibration, the event reconstruction, and the event selection used for the K_L flux measurement. The photon, π^0 , and K_L reconstruction methods are presented. A more detailed description can be found in Ref. [21].

5.1. *CsI calibration*

The energy calibration of the CsI calorimeter was performed in three steps. An initial calibration factor to convert ADC counts into energy was calculated by using vertical cosmic rays penetrating the calorimeter and assuming an energy deposit per unit path length in cesium iodide of 5.6 MeV/cm [20]. Next, from a large statistics $K_L \rightarrow 3\pi^0$ sample, we tuned the calibration factor of each crystal by minimizing the overall width of the reconstructed K_L invariant mass distribution [22]. Finally, an absolute correction to the calibration factor was obtained by using events with π^0 of known decay positions. These data were collected in special runs with a 5 mm-thick aluminum plate placed at 3353 mm upstream of the CsI front face. Neutrons in the beam core interacted with the aluminium nuclei and generated π^0 which decayed immediately. The deposit energies of the two photons from the $\pi^0 \rightarrow 2\gamma$ decays were measured by the CsI calorimeter. We scaled the absolute calibration factor of whole crystals to make the invariant mass of the two photons the same as the nominal π^0 mass. The invariant mass distribution of these events is shown in Fig. 7.

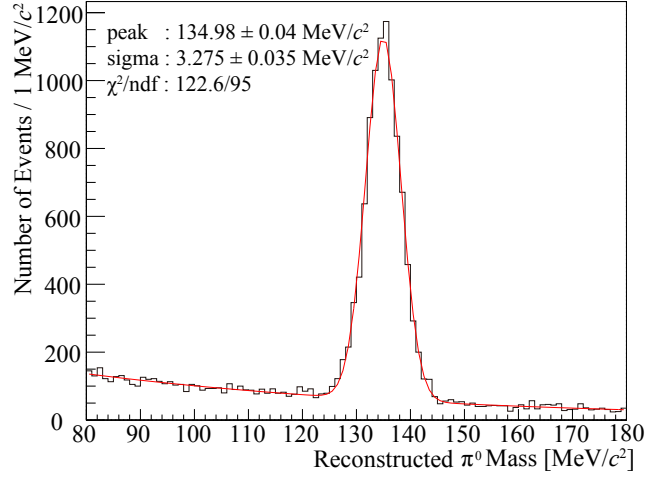


Fig. 7: Reconstructed invariant mass of π^0 events collected in the aluminum plate runs. The distribution is fitted using a Gaussian peak plus an exponential slope. The final fit is shown by the red curve.

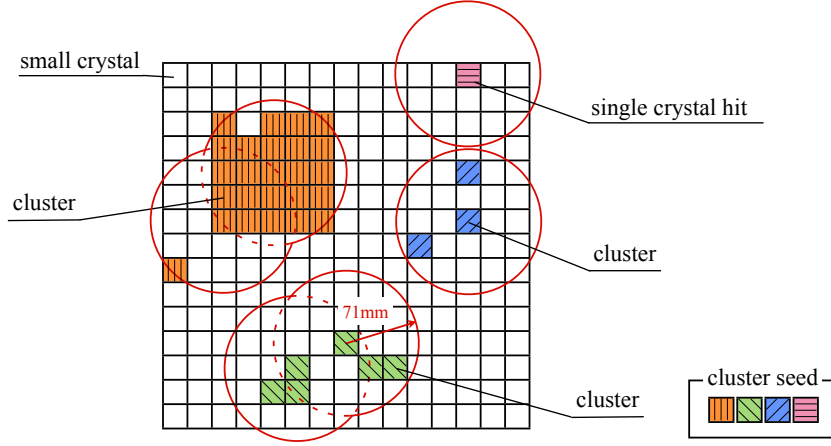


Fig. 8: Graphical view of the KOTO clustering algorithm: the colored boxes represent seed crystals. Cluster seeds with the same color share a cluster. The red circles show the cluster-growing radius of 71 mm.

5.2. Clustering

A photon hitting the CsI calorimeter induces an electromagnetic shower with a Molière radius of 3.53 cm for cesium iodide [23], thus depositing energy over multiple crystals. First, we selected CsI crystals with energy deposits above 3 MeV and within 150 ns of each other. Such crystals were called “cluster seeds”. Next we grouped seeds into a single cluster if found within 71 mm of another seed, as shown in Fig. 8. Once no other seed could be added, we

calculated the energy, coordinates, and timing of the cluster as follows:

$$E_{\text{cluster}} = \sum_{i=1}^n e_i, \quad (1)$$

$$x_{\text{cluster}} = \frac{\sum_{i=1}^n x_i e_i}{\sum_{i=1}^n e_i}, \quad (2)$$

$$y_{\text{cluster}} = \frac{\sum_{i=1}^n y_i e_i}{\sum_{i=1}^n e_i}, \text{ and} \quad (3)$$

$$t_{\text{cluster}} = \frac{\sum_{i=1}^n t_i / \sigma_{t_i}^2}{\sum_{i=1}^n 1 / \sigma_{t_i}^2}, \quad (4)$$

where n denotes the number of seeds in the cluster and e_i , x_i , y_i , and t_i are the energy, position, and time of the i th seed, respectively. The time is normalized by an energy-dependent resolution measured in test beam data as $\sigma_{t_i} = \sqrt{(5/e_i)^2 + (3.63/\sqrt{e_i})^2 + 0.13^2}$ ns, with e_i in units of MeV [13].

Clusters with more than one crystal and an energy deposit over 20 MeV were called “photon clusters” and used in the π^0 reconstruction. Single seed crystals that did not belong to any cluster were called “single-crystal hits” and used as a signature of accidentals in the CsI calorimeter.

The center of energy (x_{cluster} , y_{cluster}) was shifted from the actual incident position of the photon due to its nonzero incident angle on the surface of the CsI calorimeter, in conjunction with the depth of the main energy deposit. In addition, the energy of the cluster E_{cluster} deviated from the true photon energy due to the shower leakage outside the calorimeter. We corrected for these effects by using correction maps extracted from an MC simulation in advance. The resulting position resolution of the photon entrance position at the front face of the calorimeter was $3.7/\sqrt{E}$ [GeV] mm with a constant term of 2.1 mm.

5.3. Event reconstruction

In the analysis of $K_L \rightarrow 3\pi^0$, $K_L \rightarrow 2\pi^0$, and $K_L \rightarrow 2\gamma$ decays, the first step was to count the number of photon clusters. We required six or more photon clusters for $K_L \rightarrow 3\pi^0$, four or more photon clusters for $K_L \rightarrow 2\pi^0$, and two or more photon clusters for $K_L \rightarrow 2\gamma$ events. Next, we selected the six, four, or two photon clusters closest in time and started the process of reconstructing the K_L vertex and its four-momentum.

5.3.1. Vertex reconstruction. For $K_L \rightarrow 2\gamma$ events, the event vertex was derived assuming that the two photon clusters have an invariant mass equal to the K_L mass and originate from the beam axis at coordinates $(0, 0, Z_{\text{vtx}})$.

The reconstruction of the event vertex for $K_L \rightarrow 3\pi^0$ and $K_L \rightarrow 2\pi^0$ events started by constraining pairs of photon clusters to have an invariant mass equal to the nominal π^0 mass. The calculation of the event vertex position (X_{vtx} , Y_{vtx} , Z_{vtx}) and timing T_{vtx} follows the same principles as what was done in the E391a experiment [3]; it is outlined in the following.

Figure 9 represents a graphical description of the π^0 reconstruction. Assuming that the invariant mass of the two photons is equal to the nominal π^0 mass M_{π^0} [20], the following

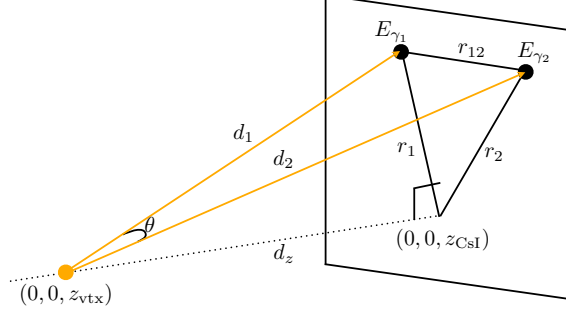


Fig. 9: Graphical description of the π^0 reconstruction: the two yellow lines show the paths of the photons from the event vertex to their entrance position at the front face of the calorimeter and θ is their opening angle; E_{γ_1} , E_{γ_2} are the energies deposited by the photons; z_{CsI} is the z position of the front surface of the CsI calorimeter in detector coordinates; d_z is the distance of the calorimeter from the event vertex; d_1 , d_2 are the distances of the two photon hits from the event vertex; and r_1 , r_2 are their projection at the front face of the calorimeter.

equation holds:

$$M_{\pi^0}^2 = 2E_{\gamma_1}E_{\gamma_2}(1 - \cos \theta), \quad (5)$$

where E_{γ_1} and E_{γ_2} are the energies of the photons and θ is the angle between their directions. In addition, the following geometrical relations hold:

$$r_{12}^2 = d_1^2 + d_2^2 - 2d_1d_2 \cos \theta, \quad (6)$$

$$d_1 = \sqrt{r_1^2 + d_z^2}, \text{ and} \quad (7)$$

$$d_2 = \sqrt{r_2^2 + d_z^2}, \quad (8)$$

where r_{12} is the distance between the hit positions of the two photons at the front face of the calorimeter and d_i (r_i) is the distance between the hit position of the i th photon and the decay vertex (z -axis). From Eqs. (5)–(8), one can calculate the distance of the π^0 from the front face of the calorimeter d_z , with an uncertainty derived from propagating the single photon energy and position resolutions. These in turn can be used to derive the position Z and uncertainty σ_z of the π^0 vertex in detector coordinates.

The six (four) photon clusters in the $K_L \rightarrow 3\pi^0$ ($K_L \rightarrow 2\pi^0$) samples can be paired to form three (two) π^0 in 15 (3) independent combinations. To find the correct photon pairing, we minimized the “pairing variance” χ_z^2 :

$$\chi_z^2 = \sum_{i=1}^n \frac{(Z_i - \bar{Z})^2}{\sigma_{zi}^2}, \quad (9)$$

$$\bar{Z} = \frac{\sum_{i=1}^n Z_i / \sigma_{zi}^2}{\sum_{i=1}^n 1 / \sigma_{zi}^2}, \quad (10)$$

where n is the number of pairs in a given combination. We assigned the \bar{Z} of the combination to the smallest χ_z^2 as the K_L decay position Z_{vtx} .

The K_L vertex position in the x - y plane was calculated as the interpolated position between the T1 target and the center of energy on the CsI front face at the position Z_{vtx} , assuming that the T1 target is a point source.

Once the three-dimensional vertex position was determined, the generated time of each photon at the vertex T_j was calculated from the photon cluster time t_j after correcting for the time-of-flight as $T_j = t_j - d_j/c$, where d_j is the distance between the event vertex and the calorimeter front face (see Fig. 9), and c is the speed of light. Finally, the time of the K_L decay time T_{vtx} was defined as the weighted mean of the photon generated times:

$$T_{\text{vtx}} = \frac{\sum_{j=1}^{2n} T_j / \sigma_{t_j}^2}{\sum_{j=1}^{2n} 1 / \sigma_{t_j}^2}, \quad (11)$$

where σ_{t_j} is the timing resolution of a cluster given by the sum in quadrature of the energy-dependent term, $3.8/\sqrt{E_j} [\text{MeV}]$ ns, and the constant term 0.19 ns.

5.3.2. Mass and momentum reconstruction. So far we have assumed that the photon pairs in $K_L \rightarrow 3\pi^0$ and $K_L \rightarrow 2\pi^0$ decays have the nominal π^0 mass. With the reconstructed vertex position in hand, these constraints were removed and the four-momenta of the π^0 were recalculated by assuming the vertex position (X_{vtx} , Y_{vtx} , Z_{vtx}). The four-momentum of the initial K_L was obtained by summing over the four-momenta of the π^0 . For the $K_L \rightarrow 2\gamma$ decay, the four-momentum of K_L was calculated from the four-momenta of the two photons assuming the vertex position (0, 0, Z_{vtx}).

5.4. Event selection

The selection of $K_L \rightarrow 3\pi^0$ events by requiring exactly six photon clusters in the CsI calorimeter resulted in a sample with 10% background contamination in the MC simulation. A similar requirement of exactly four photon clusters for $K_L \rightarrow 2\pi^0$ events, and exactly two for $K_L \rightarrow 2\gamma$ events, resulted in signal-to-background ratios of 0.18% and 0.25%, respectively. Selection criteria (cuts) on the kinematics of the event and in the presence of extra particles were applied for each mode to improve the signal-to-background ratio, as described in Sects. 5.4.1 and 5.4.2. Most cuts are common to all modes, as summarized in Tables 3, 4, and 5.

5.4.1. Kinematic cuts.

- ΔT_{vtx} cut

The difference between the time T_j of each photon in Eq. (11) and the reconstructed vertex time T_{vtx} was required to be less than 3 ns. This cut reduced the contamination of accidentals in signal events.

- $(X_{\text{min}}, Y_{\text{min}})$ cut

The position of the innermost photon was required to be outside an area of 120 mm \times 120 mm from the CsI calorimeter center. This cut removed photons whose shower leaked into the beam hole.

- R_{max} cut

The position of the outermost photon was required to be inside a radius of 850 mm from the center of the CsI calorimeter. This cut removed photons whose shower leaked outside the calorimeter fiducial volume. In the $K_L \rightarrow 2\gamma$ analysis, the outermost photon

was also required to have a minimum radius of 450 mm in order to remove background events from the $K_L \rightarrow 3\pi^0$ mode decaying near the front face of the CsI calorimeter.

- E_{\min} cut

The energy of each photon was required to be larger than 50 MeV. This cut removed photon clusters with poor energy and position resolutions.

- d_{\min} cut

The distance between the hit position of any two photons at the front face of the CsI calorimeter was required to be larger than 150 mm. This cut reduces the probability of misreconstructing a single photon into multiple clusters or multiple photons into a single cluster.

- χ_{shape}^2 cut

In order to distinguish electromagnetic showers generated by single photons from showers generated by multiple photons or hadronic interactions, we defined the cluster shape variable:

$$\chi_{\text{shape}}^2 = \frac{1}{N} \sum_{i=1}^N \left(\frac{E_i^{\text{obs}} - E_i^{\text{ref}}}{\sigma_i^{\text{ref}}} \right)^2, \quad (12)$$

where N is the number of crystals involved in the cluster, $E_i^{\text{obs}}(E_i^{\text{ref}})$ denotes the observed (expected) energy deposit in each crystal, and σ_i^{ref} is the uncertainty on the expected energy deposit. The single-crystal energy deposit, and its uncertainty, were derived from an MC simulation by using photons of different incident energies and polar and azimuthal angles [7]. A cut of $\chi_{\text{shape}}^2 < 5$ was used for the $K_L \rightarrow 2\pi^0$ and $K_L \rightarrow 2\gamma$ events.

- ΔM_{π^0} cut

The reconstructed invariant mass of the π^0 was required to be within 10 MeV/ c^2 of the nominal M_{π^0} for the $K_L \rightarrow 3\pi^0$ mode and within 6 MeV/ c^2 for the $K_L \rightarrow 2\pi^0$ mode. This cut rejected background events with mispaired photon clusters.

- ΔM_{K_L} cut

The reconstructed invariant mass for $K_L \rightarrow 2\pi^0$ events was required to be within 15 MeV/ c^2 of the nominal K_L mass [20]. This cut was effective for removing $3\pi^0$ background events with two photons not reconstructed inside the CsI calorimeter fiducial volume.

- $P_T(K_L)$ cut

The reconstructed K_L transverse momentum for the $K_L \rightarrow 2\gamma$ decay mode was required to be less than 50 MeV/ c , higher than the 30-MeV/ c peak observed in the $P_T(K_L)$ distribution of simulated events. This cut rejected background events, in particular from the $K_L \rightarrow 3\pi^0$ mode, where some missing transverse momentum was carried away by undetected particles.

- Z_{vtx} cut

The reconstructed K_L vertex was bounded to be between 2000 mm and 5400 mm in the detector coordinate for the $K_L \rightarrow 3\pi^0$ and the $K_L \rightarrow 2\pi^0$ modes, and between 2000 mm and 5000 mm for the $K_L \rightarrow 2\gamma$ mode.

- $(X_{\text{coe}}, Y_{\text{coe}})$ cut

The event center-of-energy, given by the energy-weighted x and y coordinates of all photons at the front face of the calorimeter, was required to be within a $60 \times 60 \text{ mm}^2$

area around the center of the calorimeter. This cut helped to reject background events with missing energy coming from undetected particles in the $K_L \rightarrow 2\pi^0$ mode.

- $\Sigma E_{1/2}$ cut

The sum of the energy deposited by photons in both the left and right halves of the CsI calorimeter was required to be above 350 MeV, above the trigger threshold of 307.5 MeV.

5.4.2. Veto cuts.

- CsI veto

In addition to measuring energies and positions of photons, the CsI calorimeter also served as a veto detector for extra photons. Events were removed if one or more photon clusters were present in addition to the six, four, and two photons for the $K_L \rightarrow 3\pi^0$, $K_L \rightarrow 2\pi^0$, and $K_L \rightarrow 2\gamma$ modes, respectively. The additional photon cluster was counted only if its timing was within ± 10 ns of the average time of the photon clusters used in the event reconstruction.

- CsI single-crystal hit veto

Events with “single-crystal hits” not included in any cluster were rejected. Fluctuations in the electromagnetic shower occasionally result in single crystal hits near a photon cluster. To avoid signal acceptance loss, the minimum energy threshold E_{thr} for a single-crystal hit was determined as a function of the distance from the closest photon cluster, d , as:

$$E_{\text{thr}} = (23.4 - 0.034 d[\text{mm}]) \text{ MeV} \quad \text{for } 100 < d < 600 \text{ mm}, \quad (13)$$

$$E_{\text{thr}} = 3 \text{ MeV} \quad \text{for } d \geq 600 \text{ mm}. \quad (14)$$

Furthermore, the time of the single-crystal hit was required to be within ± 10 ns of the closest photon cluster. We did not veto events with any activity within 100 mm of the photon clusters.

- CV veto

Penetrating charged particles deposit around 0.5 MeV in the CV. Based on this condition and the typical CV timing resolution (see Sect. 2.2), we defined a “CV hit” as any activity in a strip with a minimum energy deposit of 0.4 MeV in a time window of ± 10 ns from the event vertex T_{vtx} , after correcting for particle time-of-flight. The energy and timing of the hit were calculated from the sum of the energy deposit and the average of the time measured at the two ends of the CV strip, respectively. By rejecting events with any hits in the CV, background events with charged particles were effectively suppressed.

- Inner MB veto

The role of the inner MB veto was to veto the $K_L \rightarrow 3\pi^0$ background for the $K_L \rightarrow 2\pi^0$ and $K_L \rightarrow 2\gamma$ modes. The energy threshold was set at 5 MeV, and the time window, corrected for time-of-flight analogously to what was done for the CV, covered the interval $[-26, +34]$ ns. The inner MB timing resolution was 1.3 ns for a 5-MeV energy deposit. A wide time window was chosen to allow for time differences between the MB and the CsI calorimeter due to the MB length (5.5 m) along the beam direction. The energy, position, and time of a hit within the MB, after correcting for attenuation effects and the propagation delay in the WLSFs, were calculated using the signals from both the

Table 3: Cuts used in the selection for the $K_L \rightarrow 3\pi^0$ mode

Kinematic cut	Min.	Max.
ΔT_{vtx}		3 ns
$(X_{\text{min}}, Y_{\text{min}})$	120 mm	
R_{max}		850 mm
E_{min}	50 MeV	
d_{min}	150 mm	
ΔM_{π^0}		10 MeV/ c^2
ΔM_{K_L}		15 MeV/ c^2
Z_{vtx}	2000 mm	5400 mm
$\Sigma E_{1/2}$	350 MeV	
Veto cut	Energy thresh.	Time window
CsI	20 MeV	-10 ns - +10 ns

upstream and downstream ends of a MB module as:

$$t_{\text{MB}} = \frac{t_{\text{up}} + t_{\text{down}}}{2}, \quad (15)$$

$$z_{\text{MB}} = \frac{t_{\text{up}} - t_{\text{down}}}{2} \times v_{\text{prop}}, \text{ and} \quad (16)$$

$$E_{\text{MB}} = \frac{e_{\text{up}}}{\exp[-z_{\text{MB}}/(\Lambda + \alpha z_{\text{MB}})]} + \frac{e_{\text{down}}}{\exp[z_{\text{MB}}/(\Lambda - \alpha z_{\text{MB}})]}, \quad (17)$$

where $e_{\text{up}}(e_{\text{down}})$ is the visible energy and $t_{\text{up}}(t_{\text{down}})$ the hit time at the upstream (downstream) side, z_{MB} is the hit position along the beam axis with respect to the center of the MB module, $v_{\text{prop}} = 168.1$ mm/ns is the propagation velocity of light in the WLSF, and $\Lambda = 4923$ mm and $\alpha = 0.495$ parameterize the effects of the attenuation of the signal along the length of the MB.

6. Results

In this section we derive the result of the K_L flux from the measured K_L yield in each of the $K_L \rightarrow 3\pi^0$, $K_L \rightarrow 2\pi^0$, and $K_L \rightarrow 2\gamma$ samples, after normalizing to the known number of protons on target. The K_L yield Y is defined as $Y = N_{\text{rec}}^{\text{data}}/(A \times \text{BF})$ where $N_{\text{rec}}^{\text{data}}$ is the number of reconstructed data events after applying all the selection cuts and the background subtraction that is described in this section. A is the product of the decay probability and the acceptance calculated as the ratio of MC events passing the selection cuts over the total number of K_L that passed the beam exit and decayed to the given decay mode, and BF is the branching fraction for the specific decay mode listed in Table 2. In the following sections, the inputs to the yield measurement for each of the three modes are presented.

6.1. K_L yield for $K_L \rightarrow 3\pi^0$ mode

The reconstructed invariant mass distribution for $K_L \rightarrow 3\pi^0$ candidate events after applying all the selection cuts in Table 3, except for the ΔM_{K_L} cut, is shown in Fig. 10. The MC distributions in the figure are normalized so that the number of reconstructed events after applying all the selection cuts in the MC simulation with the background contamination is

Table 4: Cuts used in the selection for the $K_L \rightarrow 2\pi^0$ mode

Kinematic cut	Min.	Max.
ΔT_{vtx}		3 ns
$(X_{\text{min}}, Y_{\text{min}})$	120 mm	
R_{max}		850 mm
E_{min}	50 MeV	
d_{min}	150 mm	
χ_{shape}^2		5
ΔM_{π^0}		6 MeV/ c^2
ΔM_{K_L}		15 MeV/ c^2
Z_{vtx}	2000 mm	5400 mm
$(X_{\text{coe}}, Y_{\text{coe}})$		60 mm
$\Sigma E_{1/2}$	350 MeV	
Veto cut	Energy thresh.	Time window
CsI	20 MeV	−10 ns − +10 ns
CsI single-crystal hit	3–20 MeV	−10 ns − +10 ns
CV	0.4 MeV	−10 ns − +10 ns
Inner MB	5 MeV	−26 ns − +34 ns

Table 5: Cuts used in the selection for the $K_L \rightarrow 2\gamma$ mode

Kinematic cut	Min.	Max.
ΔT_{vtx}		3 ns
$(X_{\text{min}}, Y_{\text{min}})$	120 mm	
R_{max}	450 mm	850 mm
χ_{shape}^2		5
$P_T(K_L)$		50 MeV/ c
Z_{vtx}	2000 mm	5000 mm
$\Sigma E_{1/2}$	350 MeV	
Veto cut	Energy thresh.	Time window
CsI	20 MeV	−10 ns − +10 ns
CsI single-crystal hit	3–20 MeV	−10 ns − +10 ns
CV	0.4 MeV	−10 ns − +10 ns
Inner MB	5 MeV	−26 ns − +34 ns

equal to that in the data. The background contamination was estimated to be less than 0.1%, smaller than both the statistical uncertainty (0.39%) and the uncertainty in the nominal BF (0.61% [20]). The final number of reconstructed events in the data and the MC acceptance are listed in Table 6. The K_L yield at the beam exit for the $K_L \rightarrow 3\pi^0$ mode was estimated to be $(7.835 \pm 0.033) \times 10^8$. The uncertainty includes only the statistical uncertainties in the data and MC inputs.

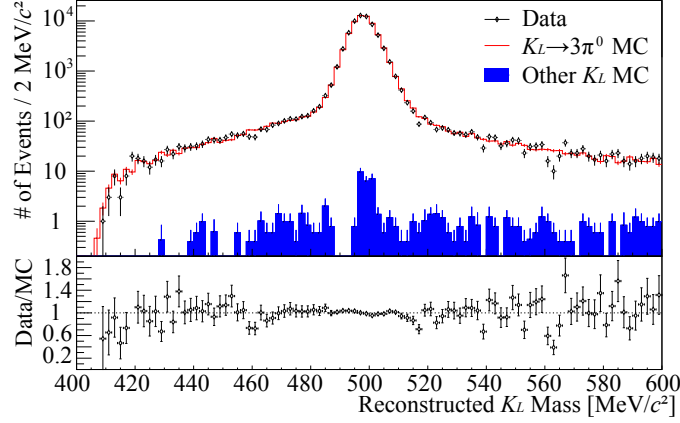


Fig. 10: Reconstructed K_L mass spectrum in the $K_L \rightarrow 3\pi^0$ data sample. The black points represent the experimental data, the open red histogram represents the $K_L \rightarrow 3\pi^0$ MC simulation, and the solid blue histogram represents the estimated contribution from the other K_L decay modes. The lower plot shows the ratio between the experimental data and the MC simulation. The error bars reflect only the statistical uncertainties.

Table 6: Number of reconstructed events in the data after applying all the selection cuts for the $K_L \rightarrow 3\pi^0$ mode and subtracting the background contamination. The MC acceptance for the signal and the dominant background contribution, before and after correcting for their BF's are also listed. The uncertainty in the acceptance reflects only the MC statistics. The last column shows the relative contribution of MC events for each decay mode.

$N_{\text{rec}}^{\text{data}}$	$65,284 \pm 256$		
	A	$A \times \text{BF}$	(%)
$K_L \rightarrow 3\pi^0$	$(4.269 \pm 0.007) \times 10^{-4}$	$(8.332 \pm 0.013) \times 10^{-5}$	99.95
$K_L \rightarrow \pi^+\pi^-\pi^0$	$(1.74 \pm 0.19) \times 10^{-7}$	$(2.18 \pm 0.23) \times 10^{-8}$	0.03

6.2. K_L yield for $K_L \rightarrow 2\pi^0$ mode

The reconstructed invariant mass distribution for $K_L \rightarrow 2\pi^0$ candidate events after applying all the selection cuts in Table 4, except for the ΔM_{K_L} cut, is shown in Fig. 11. The MC distributions in the figure are normalized to the yield measured for the $K_L \rightarrow 3\pi^0$ mode. The background contamination was estimated by minimizing:

$$\chi^2 = \sum_{i=1}^N \frac{(d_i - \alpha s_i - \beta b_i)^2}{(\sigma_{d_i})^2 + (\alpha \sigma_{s_i})^2 + (\beta \sigma_{b_i})^2} \quad (18)$$

with respect to the signal and background scale factors, α and β . Here, N is the number of bins, $d_i \pm \sigma_{d_i}$ is the number of data events in the i th bin and its statistical uncertainty, and $s_i \pm \sigma_{s_i}$ ($b_i \pm \sigma_{b_i}$) is the number of MC signal (background) events and their relative uncertainties normalized to the $K_L \rightarrow 3\pi^0$ flux result. The χ^2 minimization returned $\alpha = 0.993 \pm 0.034$ and $\beta = 0.956 \pm 0.036$ with χ^2/ndf (number of degrees of freedom) = 53.3/48. The calculated number of background events was 120.8 ± 6.2 out of 1129 total $K_L \rightarrow 2\pi^0$ candidate events.

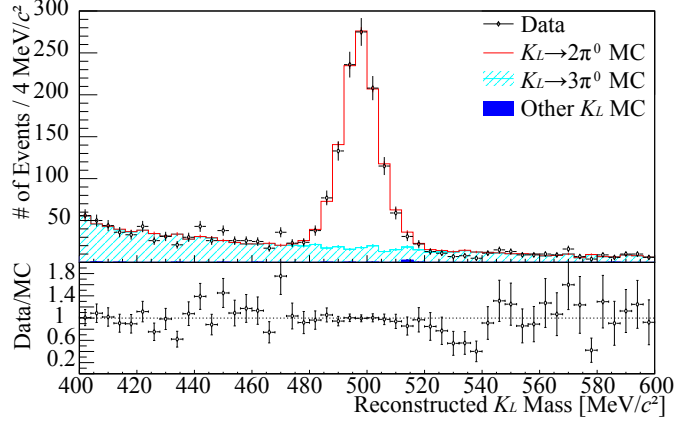


Fig. 11: Reconstructed K_L mass spectrum in the $K_L \rightarrow 2\pi^0$ selected data sample. The black points represent the experimental data, the open red histogram represents the $K_L \rightarrow 2\pi^0$ MC simulation, the light-blue histogram represents the estimated contribution from the $K_L \rightarrow 3\pi^0$ mode, and the solid blue histogram represents the contribution from the other K_L decay modes. The lower plot shows the ratio between the experimental data and the MC simulation. The error bars reflect only the statistical uncertainties.

Table 7: Number of reconstructed events in the data after applying all the selection cuts for the $K_L \rightarrow 2\pi^0$ mode and subtracting the background contamination. The MC acceptances for the signal and the dominant background contribution, before and after correcting for their respective BF's are also listed. The uncertainty in the acceptance reflects only the MC statistics. Only the backgrounds contributing more than 0.1% are listed; their relative contributions are shown in the last column.

$N_{\text{rec}}^{\text{data}}$	1008.2 ± 34.2		
	A	$A \times \text{BF}$	(%)
$K_L \rightarrow 2\pi^0$	$(1.487 \pm 0.012) \times 10^{-3}$	$(1.284 \pm 0.011) \times 10^{-6}$	88.8
$K_L \rightarrow 3\pi^0$	$(8.23 \pm 0.29) \times 10^{-7}$	$(1.606 \pm 0.056) \times 10^{-7}$	11.1

The number of reconstructed signal events and the MC acceptance are summarized in Table 7. The K_L yield at the beam exit using the $K_L \rightarrow 2\pi^0$ mode was estimated to be $(7.85 \pm 0.27) \times 10^8$. The uncertainty includes only the statistical uncertainties in the data and MC inputs.

6.3. K_L yield for $K_L \rightarrow 2\gamma$ mode

The reconstructed transverse-momentum distribution for $K_L \rightarrow 2\gamma$ candidate events after applying all the selection cuts in Table 5, except for the $P_T(K_L)$ cut, is shown in Fig. 12. The MC distributions in the figure are normalized to the yield measured for the $K_L \rightarrow 3\pi^0$ mode. Analogously to what was done in the $K_L \rightarrow 2\pi^0$ analysis, the background contamination in the candidate event sample was extracted by minimizing the χ^2 in Eq. (18). The minimization returned $\alpha = 0.973 \pm 0.025$ and $\beta = 1.023 \pm 0.031$ with $\chi^2/\text{ndf} = 67.1/78$. The calculated number of background events was 200.9 ± 8.4 out of 1890 total $K_L \rightarrow 2\gamma$ candidate events.

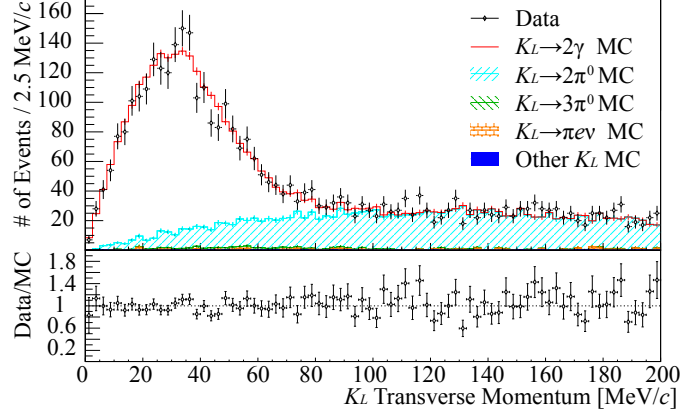


Fig. 12: Reconstructed K_L transverse-momentum spectrum in the $K_L \rightarrow 2\gamma$ selected data sample. The black points represent the experimental data, the open red histogram represents the $K_L \rightarrow 2\gamma$ MC simulation, and the light-blue, green, and orange histograms represent the estimated contribution from the $K_L \rightarrow 2\pi^0$, $K_L \rightarrow 3\pi^0$, and K_{e3} decay modes, respectively. The blue histogram represents the other K_L decay modes. The lower plot shows the ratio between the experimental data and the MC simulation. The error bars reflect only the statistical uncertainties.

Table 8: Number of reconstructed events in the data after applying all the selection cuts for the $K_L \rightarrow 2\gamma$ mode and subtracting the background contamination. The MC acceptances for the signal and the dominant background contributions, before and after correcting for their respective BF's are also listed. The uncertainty in the acceptance reflects only the MC statistics. Only backgrounds contributing more than 0.1% are listed; their relative contributions are shown in the last column.

$N_{\text{rec}}^{\text{data}}$	1689.1 ± 44.3		
	A	$A \times \text{BF}$	(%)
$K_L \rightarrow 2\gamma$	$(4.035 \pm 0.020) \times 10^{-3}$	$(2.207 \pm 0.011) \times 10^{-6}$	89.8
$K_L \rightarrow 3\pi^0$	$(1.133 \pm 0.034) \times 10^{-6}$	$(2.212 \pm 0.066) \times 10^{-7}$	9.0
$K_L \rightarrow 2\pi^0$	$(2.58 \pm 0.16) \times 10^{-5}$	$(2.23 \pm 0.14) \times 10^{-8}$	0.9
$K_L \rightarrow \pi^\pm e^\mp \nu$	$(1.4 \pm 0.4) \times 10^{-8}$	$(5.68 \pm 2.15) \times 10^{-9}$	0.2

The number of reconstructed signal events and the MC acceptances are summarized in Table 8. The K_L yield at the beam exit using the $K_L \rightarrow 2\gamma$ mode was estimated as $(7.65 \pm 0.20) \times 10^8$. The uncertainty includes only the statistical uncertainties in the data and MC inputs.

6.4. K_L flux

The measured K_L yield for each decay mode is summarized in Table 9. The three results are consistent within the statistical uncertainties. Their weighted average gives the final K_L flux of $Y_{\text{ave}} = (7.831 \pm 0.032) \times 10^8$. The uncertainty includes only the statistical uncertainty.

Table 9: K_L yield obtained for the $K_L \rightarrow 3\pi^0$, $K_L \rightarrow 2\pi^0$, $K_L \rightarrow 2\gamma$ decays, and their weighted average. The last column gives the relative yield for each decay mode with respect to the average.

Mode	K_L yield ($\times 10^8$)	Relative yield
$K_L \rightarrow 3\pi^0$	7.835 ± 0.033	1.001 ± 0.004
$K_L \rightarrow 2\pi^0$	7.85 ± 0.27	1.002 ± 0.034
$K_L \rightarrow 2\gamma$	7.65 ± 0.20	0.977 ± 0.026
Average	7.831 ± 0.032	

The absolute K_L yield in units of 2×10^{14} POT, which is the J-PARC design value for the number of protons on target per spill, was calculated from the K_L yield as:

$$\begin{aligned} \frac{\text{Number of } K_L}{2 \times 10^{14} \text{ POT}} &= \frac{Y_{\text{ave}}}{\varepsilon_{\text{trg}}} \times \frac{(2 \times 10^{14})}{N_{\text{POT}}} \\ &= (4.188 \pm 0.017) \times 10^7, \end{aligned} \quad (19)$$

where $\varepsilon_{\text{trg}} = 11.15\%$ is the KOTO trigger efficiency corrected for losses due to the DAQ dead time, and N_{POT} is the total number of protons on target collected during the run. The uncertainty includes only the statistical uncertainty of the three modes.

6.5. Systematic uncertainties

In this subsection, we describe the sources and estimation methods for the systematic uncertainties that affect the flux measurement.

The uncertainty in the signal acceptance coming from the modeling of the calorimeter was estimated by comparing the effectiveness of each kinematic and CsI veto cut in data and MC. We calculated the single-cut fractional difference, defined as the ratio of data and MC efficiency for a given cut after all others have been applied. Figure 13 shows the single-cut efficiency of data and MC and their fractional differences for all the CsI-based cuts in the $K_L \rightarrow 3\pi^0$ analysis, including the extra cluster veto cut. By summing in quadrature all the fractional differences, we obtained a total systematic uncertainty coming from the modeling of the CsI calorimeter of 1.38%. The systematic uncertainties for the other two modes were calculated in an analogous way and found to be 2.18% and 3.90% for the $K_L \rightarrow 2\pi^0$ analysis and the $K_L \rightarrow 2\gamma$ analysis, respectively. Figures 14 and 15 show the single-cut efficiencies and their fractional differences for $K_L \rightarrow 2\pi^0$ and $K_L \rightarrow 2\gamma$, respectively.

The systematic uncertainty in the acceptance from the modeling of the veto detectors' response has two components: uncertainty from accidental losses and from backplash losses. The accidental loss was due to accidental activity depositing energy in any veto detector in coincidence with a real photon in the CsI calorimeter. The backplash loss was caused by particles belonging to a photon electromagnetic shower escaping the front of the CsI calorimeter and generating secondary activity in the veto detectors. The uncertainty in the modeling of both sources was studied by comparing the efficiency of the veto detector cuts in data and MC for $K_L \rightarrow 3\pi^0$ events, for which no CV or inner MB veto cuts were applied. The change in K_L yield was measured to be 1.00% after applying the inner MB veto cut and

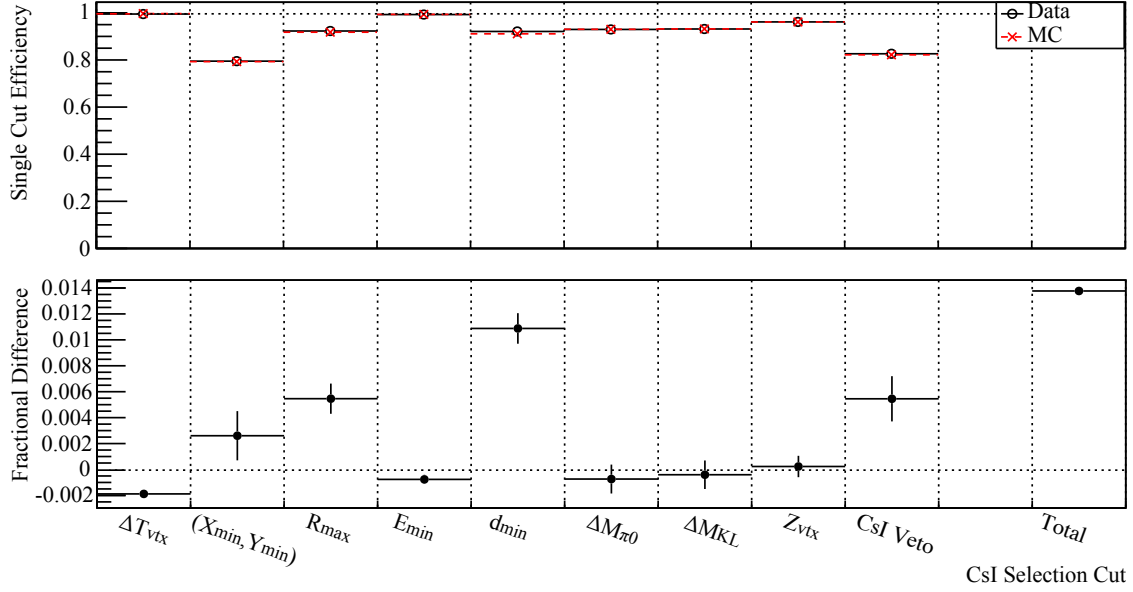


Fig. 13: Single-cut efficiency (top) and the fractional difference (bottom) for each CsI selection cut, including the extra cluster veto cut, used in the $K_L \rightarrow 3\pi^0$ analysis.

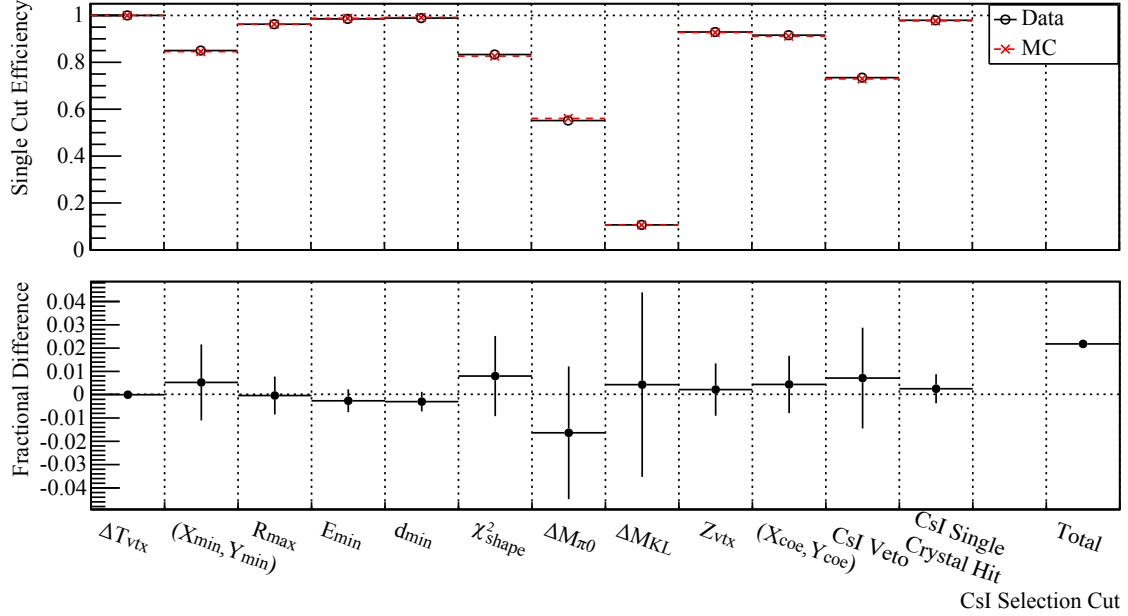


Fig. 14: Single-cut efficiency (top) and the fractional difference (bottom) for each CsI selection cut, including the extra cluster veto cut, used in the $K_L \rightarrow 2\pi^0$ analysis.

0.65% after applying the CV cut. These differences were added as systematic uncertainties in the $K_L \rightarrow 2\pi^0$ and $K_L \rightarrow 2\gamma$ selections.

Other sources of systematic uncertainties were estimated by changing the offline energy threshold from 350 MeV to the online trigger threshold value of 307.5 MeV. The resulting change in the number of selected events was taken as the systematic uncertainty of the $\Sigma E_{1/2}$

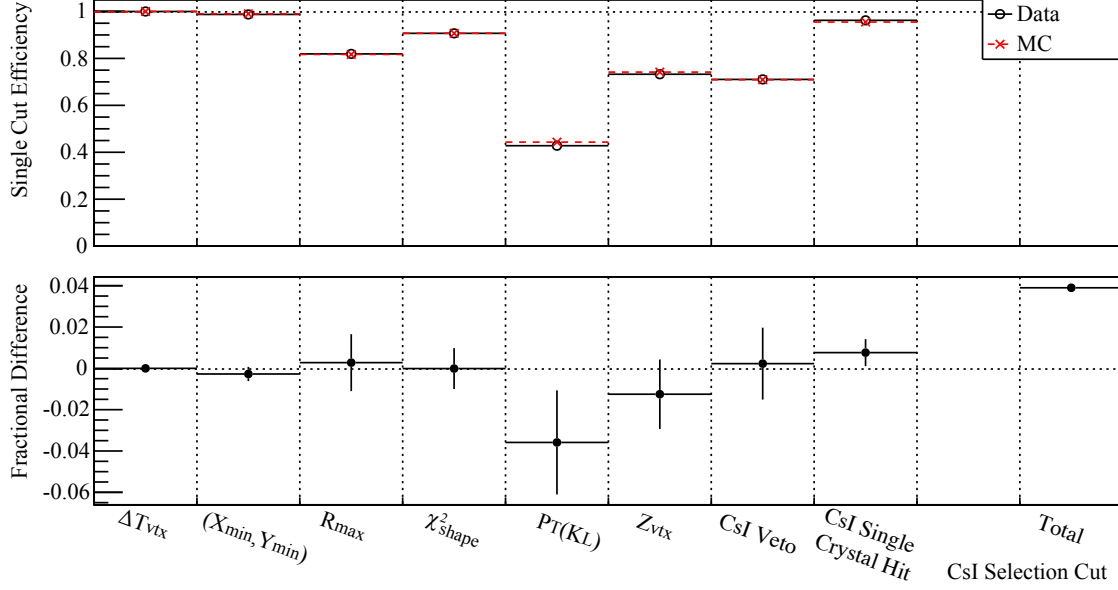


Fig. 15: Single-cut efficiency (top) and the fractional difference (bottom) for each CsI selection cut, including the extra cluster veto cut, used in the $K_L \rightarrow 2\gamma$ analysis.

cut. The K_L yield calculation used the Particle Data Group (PDG) branching fraction central values for the three neutral decay modes; the uncertainties on the central values reported in Table 2 have been considered as a source of systematic uncertainty. Finally, the conversion factor from counts in the SEC to proton intensity used in Sect. 3.2 originates the 0.39% uncertainty in the N_{POT} which is common to all the decay modes.

All the sources of systematic uncertainties are summarized in Table 10. The largest source is the modeling of the CsI calorimeter. All the other uncertainties are smaller than the statistical uncertainty for a given mode. The final uncertainty has been calculated by adding in quadrature all the statistical and mode-dependent systematic uncertainties for a single mode, taking their weighted average, and adding in quadrature the mode-independent N_{POT} uncertainty. From Eq. (19), the final K_L flux result was $(4.183 \pm 0.017_{stat.} \pm 0.059_{sys.}) \times 10^7$ K_L per 2×10^{14} protons on target. Figure 16 compares the K_L flux result separately for the three modes.

7. Discussion

The result of this paper can be compared to the previous K_L flux measurement of $(4.19 \pm 0.09^{+0.47}_{-0.44}) \times 10^7$ per 2×10^{14} POT, obtained from data taken in a dedicated beam survey run in February 2010 [6]. The experimental running conditions during the two measurements are summarized in Table 11. Although the T1 targets were made of different materials (Au in 2013 vs. Pt in 2010), they have the same proton interaction length λ_p within 3% [23].

Scaling the K_L flux measured here to the J-PARC design values of 300 kW for the beam power and 0.7-s spill duration every 3.3 s [4], we predict a K_L flux 100 times larger than that available in the previous $K_L \rightarrow \pi^0 \nu \bar{\nu}$ search experiment. Together with the upgrades to the detector, the experiment should reach the sensitivity of the standard model prediction for the $K_L \rightarrow \pi^0 \nu \bar{\nu}$ search over a period of three Snowmass years (3×10^7 s).

Table 10: Summary of the systematic uncertainties. The first five sources are added in quadrature to obtain the mode-dependent systematic uncertainty of each decay channel. The N_{POT} uncertainty is independent of the three modes.

Source	$K_L \rightarrow 3\pi^0$	$K_L \rightarrow 2\pi^0$	$K_L \rightarrow 2\gamma$
CsI calorimeter modeling	1.38%	2.18%	3.90%
Main Barrel modeling	–	1.00%	1.00%
Charged Veto modeling	–	0.65%	0.65%
$\Sigma E_{1/2}$ cut	0.24%	0.41%	0.04%
PDG branching fraction [20]	0.61%	0.69%	0.73%
Mode-dependent	1.53%	2.61%	4.14%
Mode-independent (N_{POT})	0.39%		

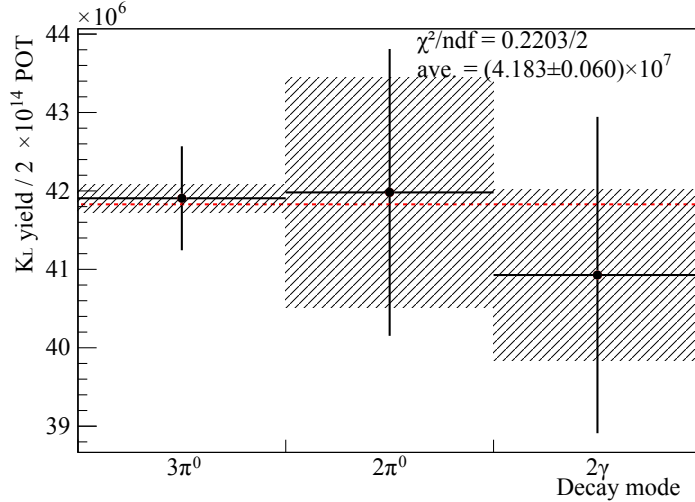


Fig. 16: K_L flux result for each of the $K_L \rightarrow 3\pi^0$, $K_L \rightarrow 2\pi^0$, and $K_L \rightarrow 2\gamma$ modes. The hatched area shows the statistical uncertainty and the vertical bar shows the quadratic sum of the statistical and mode-dependent systematic uncertainties. The horizontal dashed line shows the weighted average value.

8. Conclusion

In this paper, we have described the K_L flux measurement for the KOTO experiment with data taken during a detector commissioning run in January 2013. The measurement was done by using three K_L neutral decay modes: $K_L \rightarrow 3\pi^0$, $K_L \rightarrow 2\pi^0$, and $K_L \rightarrow 2\gamma$. The results for the three decay modes agreed with each other within the statistical uncertainties. Systematic uncertainties were estimated based on the reproducibility of the data selection efficiency in the Monte Carlo simulation. The final K_L flux was $(4.183 \pm 0.017 \pm 0.059) \times 10^7$ per 2×10^{14} protons on target, where the first uncertainty was statistical and the second was systematic. This result is in agreement with a previous measurement done by the KOTO Collaboration during a dedicated beam survey run in February 2010.

Table 11: Comparison of target material and target thickness, both in units of mm and proton interaction length λ_p , for the two KOTO K_L flux measurements. The last two columns summarize the typical beam power conditions and the K_L decay modes used for each measurement.

Period	material	Target thickness	λ_p	MR beam power	Measured mode
Feb. 2010	Pt	60.0 mm	0.658	1 kW, 1.5 kW	$K_L \rightarrow \pi^+ \pi^- \pi^0$
Jan. 2013	Au	66.0 mm (1-mm slits included)	0.640	15 kW	$K_L \rightarrow 3\pi^0$ $K_L \rightarrow 2\pi^0$ $K_L \rightarrow 2\gamma$

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